ANALYSIS OF PATIENTS FLOW IN AN EMERGENCY WARD USING FUZZY CRITICAL PATH METHOD AND FUZZY PROGRAM EVALUATION AND REVIEW TECHNIQUE (A CASE STUDY OF AMINU KANO TEACHING HOSPITAL, KANO, NIGERIA)

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ABSTRACT

In this paper, a mathematical model is proposed to handle project scheduling problem under vagueness. The intent is to model patients flow process in imprecise or vague circumstances using critical path analysis. Furthermore, the research discusses utilization of fuzzy critical path method in conjunction with fuzzy program evaluation and review technique to determine the duration required for the treatment of patients in emergency ward of Aminu Kano teaching hospital. The activities considered are those affecting patients flow during treatments in the emergency ward and the related project network is drawn. The reason for incorporating fuzzy logic in this research comes from the fact that fuzzy numbers are more reliable in dealing with ambiguous processes such as witnessed in the emergency ward of a hospital. The choice of emergency department for this work is because it is a major access point where from the beginning patients are given treatments for a wide range of sicknesses and injuries. These sicknesses and injuries may be deadly and requires prompt attention. Therefore, any delay in patient treatment in the emergency ward may result in undesired consequences and losses of lives. Findings through the application of fuzzy critical path method and fuzzy program evaluation and review technique enabled the determination of the critical path and patients' treatment expected completion time. The entire idea is to reduce unnecessary delay by eliminating unnecessary activities, thus increase the quality of treatment of patients in the hospital.

Keywords: Emergency ward, fuzzy critical path, slack times, patient treatment, fuzzy logic.

1. INTRODUCTION

A project is a unique set of tasks with defined objectives, precedence relationships, numerous activities and defined period for completion of the tasks (Gül, Güneri & Güneş, 2017). Project management deals with the conception, feasibility analysis, planning,

execution, monitoring, control, and termination of a project (Reid & Sanders, 2010). It includes stabilizing the contending desires for time, cost, quality and access to services (Gül, Güneri & Güneş, 2017).

The three main items to consider in the choice of a hospital are quality, cost and access to services. The patients consider an ideal hospital as one that provides satisfactory services with lower costs and easy access to services. The emergency ward is a sub unit in the hospital which is a major access point where from the beginning patients are given treatments for a wide range of sicknesses and injuries. These sicknesses and injuries may be deadly and requires prompt attention (McLaughlin & Hayes, 2008; Gül, Güneri & Güneş, 2017). Therefore, any delay in patient treatment time in the emergency ward may result in undesired consequences and loss of lives.

A major determinant of efficient service delivery in hospitals, especially, the emergency ward is the time required for treatment of patients (Gül, Güneri & Güneş, 2017). The patient flow procedure in the emergency ward of Aminu Kano teaching hospital (AKTH) is in the following order: walk in patient or wheel in patient, assessment and intervention by the triage personnel, registration, and clinical review by doctor. After the clinical review, the patient may be discharged, or kept for observation for 12 hours or less, or may be admitted in emergency ward for 48 hours. This is followed by sending the patient to available unit, or shifting patient to another facility, or discharged. After discharged of the patient, he or she may be given health education or sent for pharmaceutical processes, then followed by account disengagement and billing.

Different problems arise due to complexity and uncertainties involved in the listed activities performed in the emergency ward. This naturally leads to unnecessary delays in receiving treatments, poor resources utilization, and improper staff scheduling. Some of the reasons for prolonged waiting times in emergency ward are long waits to see the doctor, delay in assessment and intervention by the triage personnel, delays in carrying out tests and getting the results, and shortage of medical staff (McLaughlin & Hayes, 2008; Gül, Güneri & Güneş, 2017). Therefore, changes must be made to improve performance and encourage efficient patient flow processes of the emergency ward. Some of the needed changes are to get rid of redundant activities and identifying alternative flow processes. Luckily, two closely related operations research techniques, critical path method (CPM) and program evaluation and review technique (PERT), are readily available for use of managers of the emergency wards to assist them in carrying out these responsibilities. These techniques heavily rely on the application of project network diagrams in planning and displaying the coordination of all the activities (Hillier & Lieberman, 2001).

Szmer & Węgrzyn (2019) deduced that the efficiency of the operating ward has a great effect on the financial condition of a hospital. The operating department is estimated to provide two-thirds of the income, at the same time generate 40% of the costs. A set back in the implementation of the operation plans may results in financial losses for the whole hospital. The work focused on how to eliminate or at least reduced these delays in the operating department. Furthermore, the study had shown how efficient time management and application of other corrective measures had reduced the delays by 16%.

Gül, Güneri & Güneş (2017) identified activities affecting patient flow through the emergency department of a university teaching hospital in Turkey. Project network was drawn using fuzzy activity times obtained from the emergency department of the university hospital. Fuzzy CPM and fuzzy PERT were used to calculate the critical path, expected time, and float times for the project completion.

Jain (2013) used PERT and CPM to monitor and control health related programmes and projects. It was shown that the methods enhance the calculation of the expected projects completion time, identify the tasks and the start and finish times of activities. Furthermore, the work analyzed the impact of revising and rescheduling of the projects, delay of some activities, estimation of the resources required to complete each activity and determination of the type of extra resources needed.

Merten (1966) shows that PERT can be of great assistance to the public health manager in the precise evaluation of project progress, harmonization, logical eradication of redundant activities, allotting of responsibility for different components of the project, as well as initial and final evaluation. PERT can also be used for multiple screening, other public health projects, budget and personnel employment processes. In addition, the technique could be profitably applied to projects such as organizing different kinds of large conferences, R & D programs, immunization programs, acquiring and processing of data for essential records, and the promotion of law making (Merten, 1966).

The aim of this paper is to evaluate the patients flow in the emergency ward of AKTH using fuzzy CPM (FCPM) and fuzzy PERT (FPERT). The tools and methods used in this research are aimed at providing time and cost-effective scheduling process so as to improve patients flow. In particular, these improvements will greatly reduce delays in the duration of treatment of patients.

2. METHODOLOGY

In this section, the methodology used in this paper is described. First, the classical CPM and PERT Algorithms are discussed, and then the **F**CPM and FPERT Algorithms are also described.

2.1. CPM and PERT Algorithms

Project network is a graphical representation of logical and sequentially connected activities and events of a project. The project network is sometimes called arrow diagram. The two most widely applied network techniques are PERT and CPM. PERT and CPM are useful for planning, scheduling and executing large time-bound projects which involve careful coordination of a variety of complex and interrelated activities and resources.

Essentially, there are six steps which are common to both the techniques that are described below.

- 1) Specify the individual activities and milestones. These activities are jobs needed for the completion of a project while, milestones are significant events marking the beginning and the end of one or more activities.
- 2) Develop a logical sequence of those activities. Some of these activities are dependent upon the completion of others. The determination of the predecessor-successor relationships between the various activities of the project is useful in the construction of the network diagram. In some cases, these activities may require detailed analysis to determine the precise order in which they must be arranged. The activities are normally arranged in tabular form.
- 3) Construct a network diagram. The network diagram can now be drawn using activity sequence information. A node represents each activity in the network, while the arrow indicates the relationship between activities (see, fig. 1) and general progression in time. There exist some software packages that simplify this step by automatically converting tabular activity information into a network diagram (Hillier & Lieberman, 2001).
- 4) Determine the completion time for individual activity. Estimation of the time needed to complete each activity is done using past experience or the estimates of knowledgeable persons. Units of time for activity completion in common use are minutes, hours, weeks, days etc.

CPM is a deterministic model that does not take into account variation in the completion time, so only one number can be used to determine an activity time (Punmia & Khandelwal, 2006). In contrast, PERT is a probabilistic model and has the ability to deal with uncertainty in activity completion time. The classical PERT model usually has three time estimates (.i.e., Optimistic time, most likely time and pessimistic time).

PERT uses a beta probability distribution for the time estimates and the expected time for each activity can be calculated using (1).

$$t_{e} = \frac{t_{o} + 4t_{m} + t_{p}}{6}$$
(1),

where, $t_e =$ expected time, $t_o =$ optimistic time, $t_m =$ most likely time, and $t_p =$ pessimistic time.

According to Punmia & Khandelwal (2006), the estimated expected time for the completion of each activity is usually displayed on a network diagram.

To calculate the variance for each activity completion time, if three values are selected for standard deviation times each for the optimistic and pessimistic times; it means there are six standard deviations between them. The variance is calculated using (2).

$$\sigma^2 = \left(\frac{t_p - t_o}{6}\right)^2 \tag{2}$$

5) Identify the critical path. The critical path is the path with the longest duration through the network. It is calculated by adding all the activity time in each sequence and identify the longest path in the project. The critical path determines the total calendar time required for the project. The significance of the critical path is that the activities that lie on it cannot be delayed without delaying the project. As a result of its impact on the entire project, critical path analysis is an important aspect of project planning. If activities outside the critical path speed up or slow down (within limits), the total project time does not change. The amount of time that a non – critical path activity can be delayed without affecting the project is referred to as a slack time. Therefore, the critical path is the path in the network in which none of the activities have slack.

The critical path can easily be identified by determining the following four parameters for each activity:

- i. ES Earliest Start time
- ii. EF Earliest Finish time
- iii. LS Latest Start time
- iv. LF Latest Finish time

These times are calculated using the expected time for the relevant activities. The earliest start time is the earliest time at which an activity can begin given that its predecessor activities must be completed first. The earliest finish time is the same as the earliest start time for the activity plus the time required to complete the activity. The ES and EF are determined by working forward through the network. The latest finish time is the latest time at which an activity can be completed without delaying the project. The latest start time, equal to the latest finish time minus the time required to complete the activity. LS and LF are found by working backward through the network.

6) Update the network diagram

As the project progresses, the actual activity completion times will be ascertained and the network diagram can be updated to include this actual times. A new critical path may emerge, and structural changes may be made in the network if project requirements change. In situations where delays are visible, additional resources may be needed to be within schedule time and therefore the network diagram has to be changed to reflect the new situation.

2.2. FCPM and FPERT Algorithms

The notations and process steps of FCPM and FPERT are adopted from (Omer Atli & Cengiz Kahraman, 2012; Gül, Güneri & Güneş, 2017) as follows:

Notations

N: All nodes in a project network,

A_{ij}: The activity between two nodes (from i to j)

FAT_{ij}: Fuzzy activity time of A_{ij}

EFT: Earliest fuzzy time

LFT: Latest fuzzy time

 SFT_{ii} : The total fuzzy slack time of A_{ii}

 $FCPM(P_n)$: The fuzzy completion time of path P_n .

t: Number of activities in a project network

S(j): The set of all activities after node j.

NS(j): The set of all nodes connected to all activities after node $j = \{k / A_{ik} \in S(j), k \in N\}$

P(j): The set of all activities before node j.

NP(j): The set of all nodes connected to all activities before node $j = \{i | A_{ij} \in P(j), i \in N\}$

2.2.1. Steps for determination of FCPM

Step 1: Set initial node $EFT_1 = (0, 0, 0, 0)$.

Step 2: Evaluate β , the risk factor for each A_{ii} using (3).

$$\beta = \sum_{i} \sum_{j} \left(\frac{(b_{ij} - a_{ij})}{(b_{ij} - a_{ij}) + (d_{ij} - c_{ij})} \right) / t$$
(3)

The risk situation is neutral, if $\beta = 0.5$. If $\beta < 0.5$ it is risky and a more risky situation if $\beta > 0.5$

Step 3: Determine the ETF for individual node using (4).

$$EFT_{i} = EFT_{i} \oplus FAT_{ii} \tag{4}$$

Step 4: Take EFT_j with the highest value for each node after comparing the EFT_j s for intersecting nodes using (5).

$$EFT_{j} = \max\left\{EFT_{i} \oplus FAT_{ij}\right\} = \max\left\{(a_{x}, b_{x}, c_{x}, d_{x}), (a_{y}, b_{y}, c_{y}, d_{y})\right\}$$
(5)

Step 4(a): Evaluate the values of x_1 and x_2 using (6)

$$x_{1} = \min\{a_{x}, b_{x}, c_{x}, d_{x}, a_{y}, b_{y}, c_{y}, d_{y}\}, x_{2} = \max\{a_{x}, b_{x}, c_{x}, d_{x}, a_{y}, b_{y}, c_{y}, d_{y}\}$$
(6)

Step 4(b): Determine the values of $R((a_x, b_x, c_x, d_x))$ and $R((a_y, b_y, c_y, d_y))$ using (7)

$$R((a_i, b_i, c_i, d_i)) = \beta[(d_i - x_i) / (x_2 - x_1 - c_i + d_i)] + (1 - \beta)[1 - (x_2 - a_i) / (x_2 - x_1 + b_i - a_i)]$$
(7)

Step 4(c): Rank the results of $R((a_i, b_i, c_i, d_i))$ and take the one that is bigger.

Step 5: Determine LFT for individual node using (8)

$$LFT_{i} = EFT_{k}\Theta FAT_{ik}$$
(8)

Step 6: Consider LFT_j with the lowest value for each node after comparing the LFT_js for intersecting nodes using (9)

$$LFT_{j} = \min\left\{EFT_{k}\Theta FAT_{jk}\right\} = \min\left\{(a_{x}, b_{x}, c_{x}, d_{x}), (a_{y}, b_{y}, c_{y}, d_{y})\right\}$$
(9)

Note that the sub-steps of Step 6 are similar to that of step 4.

Step 7: Determine SFT for every activity using (10)

$$SFT_{ij} = LFT_j \Theta(EFT_i \oplus FAT_{ij}) \tag{10}$$

Step 8: Determine all possible paths and find the FCPM values for all paths. FCPM can be calculated using (11).

$$FCPM(P_n) = \sum SFT_{ij} \tag{11}$$

Step 9: Consider all FCPMs and take the minimum value as the FCPM as done in Step 6 using (12). Rank the results of $R((a_i, b_i, c_i, d_i))$ and take the one that has smaller value.

$$FCPM(P_n) = \min\{FCPM(P_i) | i = 1, 2, 3, ..., n\}$$
(12)

Step 10: Consider the path with the smallest FCPM and take it as the critical path.

2.2.2. Steps for determination of FPERT

To determine the FPERT requires finding a generalized mean and calculating the standard deviation based on trapezoidal fuzzy numbers. Generalized mean can be calculated using (13).

$$\mathbf{M}(a_1, b_1, c_1, d_1) = \frac{a_1 + b_1 + c_1 + d_1}{4}$$
(13)

The standard deviation for the trapezoidal fuzzy numbers can be calculated using (14).

$$D(a_1, b_1, c_1, d_1) = \frac{[3(a_1^2 + b_1^2 + c_1^2 + d_1^2) - 2(a_1b_1 + a_1c_1 + b_1c_1 + a_1d_1 + b_1d_1 + c_1d_1)]}{36}$$
(14)

After the critical path is determined, the next thing is to find the probability of meeting the scheduled completion time of a patient treatment. When activities of the project are large, as with the PERT projects then the expected time of individual activities has random probability distribution and the variation of the expected time for the project is completely assumed to have a normal distribution. This assumption of normal probability distribution is based on central limit theorem (Punmia & Khandelwal, 2006).

The probability factor (Z) is called normal deviate which is the distance from the mean expressed in terms of standard deviation σ (Punmia & Khandelwal, 2006). Z may be positive, zero or negative. If Z > 0, then the probability of completing a project in time is more than 0.5, if Z = 0, then the probability of completing the project in time is 0.5 and if Z < 0 then the probability of completing the project in time is 0.5.

The mean and standard deviation of the normal probability distribution are used for the calculation of Z using relation (15).

$$Z = \frac{X - \mu}{\sigma} \tag{15}$$

3. A CASE STUDY

A case study is performed in the emergency ward of Aminu Kano teaching hospital (AKTH), Kano, Nigeria. The activities and sequence of patients flow in the emergency department is shown on table 1. FATs in respect of each activity in the treatment of patient in emergency ward is shown on table 2, while the project network chart for the treatment of patient is shown in figure 1.

Symbol	Activity
А	Moving of the patient from ambulance or private car to emergency ward
В	Walk in patient or wheel in patient
С	Assessment and intervention by the triage personal
D	Registration
Е	Clinical Review
F	Sending the patient to available unit in the hospital determined by the
	severity of illness
G	Change the patient to a new facility
Н	Discharge

Table 1. Activities for the Treatment of Patient in Emergency Department

Ι	Health Education
J	Pharmaceutical processes
K	Account Disengagement
L	Receive bill for services rendered

Table 2. FATs for every activity for treatment of patient in emergency ward

Activity	Predecessor	FAT	ls (in m	inutes)	
А	-	3	4	4.5	5
В	А	0.5	1	1.5	2
С	В	0.5	1	2	4
D	С	10	12	15	30
Е	D	10	20	30	40
F	E	440	1920	2400	2880
G	Е	30	40	60	90
Н	F,G	30	60	90	120
Ι	Н	3	4	5	6
J	Ι	6	10	15	20
K	Ι	5	8	10	15
L	K	30	45	120	180



Figure 1: Project Network Chart for the Treatment of Patient in Emergency Ward

In this work, trapezoidal fuzzy numbers are used to represent the fuzzy activity times. The a_{ij} and d_{ij} are the lowest and highest values of evaluating activity time for A_{ij} , whereas b_{ij} and c_{ij} represent the first and third quartile respectively of activity time for A_{ij} . Suppose that only one set of four data; a_{ij}, b_{ij}, c_{ij} and d_{ij} is obtained, and then this data can be arranged from the lowest to highest. If on the other hand, no information is obtained in respect of activity A_{ij} , then the $FAT_{ij} = (a_{ij}, b_{ij}, c_{ij}, d_{ij})$ will be determined subjectively by the manager of the emergency ward based on his or her experience.

Computations of EFT and LFT Values

The values of EFT and LFT are calculated for each node by using appropriately equations (8), (9), (10), (11) and (12). The results of these computations are shown on table 3 and table 4.

NODE	EFT Values				
1	0	0	0	0	
2	3	4	4.5	5	
3	3.5	5	6	7	
4	4	6	8	11	
5	14	18	23	41	
6	24	38	53	81	
7	24	38	53	81	
8	464	1958	2453		
	2961				
9	494	2018	2543		
	3081				
10	497	2022	2548		
	3087				
11	497	2022	2548		
	3087				
12	503	2032	2563		
	3107				
13	533	2077	2683		
	3287				

Table 3. EFT Values

NODE		LF	T Values
1	-2754	-606	606
	2754		
2	-2749	-601.5	610
	2757		
3	-2747	-600	611
	2757.5		
4	-27 43	-598	612
	2758		
5	-2713	-583	624
	2768		
6	-2673	-553	644
	2778		
7	-2673	-553	644
	2778		
8	207	1847	2564
	3218		
9	327	1937	2624
	3248		
10	333	1942	2628
	3251		
11	333	1942	2628
	3251		
12	353	1957	2638
	3257		
13	533	2077	2683
	3287		

Table 4. LFT Values

Computations of SFT Values

The total SFTs are calculated for each activity using (12), the results of the calculations are shown on table 5.

Table 5. SFT ValuesSFTVALUES

1-2	-2754	-606	606	
	2754			
2-3	-2754	-606	606	
	2754			
3-4	-2754	-606	606	
	2754			
4-5	-2754	-606	606	
	2754			
5-6	-2754	-606	606	
	2754			
6-7	-2754	-606	606	
	2754			
6-8	-2754	-606	606	
	2754			
7-8	36	1734	2486	
	3164			
8-9	-2754	-606	606	
8-9	-2754 2754	-606	606	
8-9 9-10	-2754 2754 -2754	-606 -606	606 606	
8-9 9-10	-2754 2754 -2754 2754	-606 -606	606 606	
8-9 9-10 10-11	-2754 2754 -2754 2754 -2754 -2754	-606 -606 -606	606 606 606	
8-9 9-10 10-11	-2754 2754 -2754 2754 -2754 -2754 2754	-606 -606 -606	606 606 606	
8-9 9-10 10-11 10-12	-2754 2754 -2754 2754 -2754 2754 2754 -2754	-606 -606 -606 -601	606 606 606 608	
8-9 9-10 10-11 10-12	-2754 2754 -2754 2754 -2754 2754 -2754 -2749 2755	-606 -606 -606 -601	606 606 606 608	
8-9 9-10 10-11 10-12 11-12	-2754 2754 -2754 2754 -2754 2754 -2754 2755 -2754	-606 -606 -601 -606	606 606 608 606	
8-9 9-10 10-11 10-12 11-12	-2754 2754 -2754 2754 -2754 2754 -2754 2755 -2754 2754	-606 -606 -601 -606	606 606 608 606	
8-9 9-10 10-11 10-12 11-12 12-13	-2754 2754 -2754 2754 -2754 2754 -2754 2755 -2754 2755 -2754 2754 -2754	-606 -606 -601 -606 -606	606 606 608 606 606	

Determination of Critical Paths

When all possible paths are found, then FCPMs for each node are evaluated using (11). The results are compared and FCPM (P_i) is obtained using (3) in Step 4. The calculated values for FCPM and R[FCPM (P_i)] of every path obtained are presented on table 6.

Table 6. FCPM AND R (FCPM (P_i)) values of each possible path

#	Possible paths		FCF	$PM(P_i)$		R
1	1-2-3-4-5-6-7-8-9-10-11-12-	-30258	-4932	9152	33458	0.4855
13						
2	1-2-3-4-5-6-7-8-9-10-12-13	-27499	-4321	8548	30705	0.4884
3	1-2-3-4-5-6-8-9-10-11-12-	-30294	-6666	6666	30294	0.4638
13						
4	1-2-3-4-5-6-8-9-10-12-13	-27535	-6055	6062	27541	0.4662

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It can be seen from table 6 that the critical path is 1 - 2 - 3 - 4 - 5 - 6 - 8 - 9 - 10 - 11 - 12 - 13, since R (FCPM (P_2)) has the lowest value of all possible paths. Therefore, it can be concluded that the length of treatment time lies approximately between 2077 and 2683 minutes i.e. (533, 2077, 2683, 3287), which is equivalent to between 34.62 to 44.72 hours.

Determination of FPERT

In the determination of FPERT, the computation of the generalized mean value for each activity can be done using (13) and (14) as shown on table 7.

Activity	Α	В	С	D	Mean
Α	3	4	4.5	5	4.1250
В	0.5	1	1.5	2	1.2500
С	0.5	1	2	4	1.8750
D	10	12	15	30	16.7500
E	10	20	30	40	25.0000
F	440	1920	2400	2880	1910.0000
G	30	40	60	90	55.0000
Н	30	60	90	120	75.0000
Ι	3	4	5	6	4.5000
J	6	10	15	20	12.7500
K	5	8	10	15	9.5000
L	30	45	120	180	93.7500
Total					2115.7500
Activities of					2051.2500
ср					

Table 7. Mean for each activity

Activity	A	b	С	D	Variance
А	3	4	4.5	5	0.2431
В	0.5	1	1.5	2	0.1389
С	0.5	1	2	4	0.7986
D	10	12	15	30	27.4167
Е	10	20	30	40	55.5556
F	440	1920	2400	2880	371333.3333
G	30	40	60	90	233.3333
Н	30	60	90	120	500.0000
Ι	3	4	5	6	0.5556
J	6	10	15	20	12.3056
K	5	8	10	15	5.8889
L	30	45	120	180	1618.7500
Total					373788.3196
Activities of					373549.0974
ср					

Table 8. Variance for each activity

Computation of standard deviation with sum of variance of activities on the critical path is performed and the result is

$$\sigma = \left(\sum \sigma_{ij}^2\right)^{\frac{1}{2}} = \left(373549.0974\right)^{\frac{1}{2}} = 611.1866$$

Computation of expected completion time with sum of mean of activities on the critical path gives

$$\mu = \sum m_{ij} = 2051.2500$$

The calculated values of mean and standard deviation of the normal probability distribution are used to determine various values of Z using relation (16) and the results are shown on table 9.

Table 9. Some probabilities of the project completion tin

Х	Z Values	Probability
<1800	-0.4111	0.3409

<2000	-0.0839	0.4681
<2200	0.2434	0.5948
< 2400	0.5706	0.7157
<2600	0.8978	0.8159
<2800	1.2251	0.8907
<3000	1.5523	0.9394
<3200	1.8795	0.9699
<3400	2.2068	0.9864
<3600	2.5340	0.9943
<3800	2.8612	0.9979
<4000	3.1885	0.9993
<4200	3.5157	0.9998
<4400	3.8429	0.9999

4. Discussion of results

The Case study describes a patient treatment project which includes 12 subactivities as shown on Table 1.The details of the activities and their predecessor relationships are presented in column 1 and 2 of Table 2 while, the details of the activities and time estimates of activity durations are also shown in columns 3, 4, 5 and 6 of table 2.

It was found that the critical path is 1-2-3-4-5-6-8-9-10 -11-12-13, since R (FCPM (P_2)) has the lowest value of all possible paths. Therefore, it can be concluded that the length of treatment time lies approximately between 2077 and 2683 minutes.

The critical path was found to consist of the following activities: A (Moving of the patient from ambulance or private car to emergency ward), B (Walk in the patient or wheel in the patient to the ward), C (Assessment and intervention by the triage personal), D (Registration), E (Clinical Review), F (Sending the patient to available unit in the hospital depending on the severity of illness), H (Discharge), I (Health Education), J(Pharmaceutical processes), K(Account Disengagement) and L (Receive bill for services rendered).

Punmia and Khandelwal (2006) established that the critical path does not allow any flexibility in critical activities. As a change in any of the critical activities A, B, C, D, E, F, H, I, J, K or L on the critical path will negatively affect the entire treatment time of patients in the emergency ward.

Table 9 gives the values of Z, with some probabilities of the treatment completion time of a patient. As noted in the first and last columns, the probability of completing the treatment of the patient in less than 3200 minutes is 96.99%, in less than 3400 minutes is 98.64%, in less than 3600 minutes is 99.43%, in less than 3800 minutes is 99.79%, in less than 4000 minutes is 99.93%, in less than 4200 minutes is 99.98%, and in less than 4400 minutes is 99.99%.

It can be observed that the probability of completing the treatment of the patient in less than 2200 minutes (59.48%) and in less than 2800 minutes (89.07%) is within the probable range. This was found to be approximately between 2077 and 2683 minutes (equivalent of 34.62 to 44.72 hours) through the use of FCPM. Therefore, the treatment of a patient will be completed before the 44.72 hours, even after taking into consideration of the worst case scenario.

5. Conclusion

This paper presents the patients treatment evaluation project scheduling in AKTH using CPM and PERT techniques. These techniques provide both the deterministic and probabilistic models used in the planning, scheduling and controlling the patients' treatment durations.

Project network analysis had been used as a major tool to efficiently analyze the number of hours taken to complete the treatment of a patient in the emergency department of AKTH. Investigation through this research revealed that 1600 patients can be treated in at least 55,392 hours and at most 71,552 hours in the emergency ward of AKTH.

This work is done to significantly reduce delays in the duration of treatments, weed out redundant activities at the same time increase the quality of treatment of patients. The effectiveness of the emergency ward will largely depends on the skillful management of time in relation to patient flow processes.

In the evaluation of patient flow of the emergency department, PERT method was used to check the Pessimistic Time (longest time possible and can be seen as usual delay), Most Likely Time (the time the activity would often require if normal conditions prevailed) and Optimistic Time (shortest time possible if things go perfectly) as well as the probability of completing the treatments within a specific time.

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